

Sub-Hinze bubble production in turbulence

S. Perrard*, A. Rivière*, D. J. Ruth‡, W. Mostert†§,
L. Duchemin*, C. Josserand¶, L. Deike†||

Liquid-gas flows play a central role in the transfert of low solubility gases, such as CO₂, from the atmosphere to the ocean¹². Indeed, when a wave breaks, it traps large volumes of air that will fragment and generate sub-millimetric bubbles. This fragmentation dynamics is controlled by the Weber number We , the ratio between inertial force and capillary force. A critical break up size, the Kolmogorov-Hinze scale d_h corresponding to a Weber of order unity separates stable bubbles ($d \ll d_h$) from bubbles that will surely break ($d \gg d_h$). The sub-Hinze bubbles in particular rise slower to the surface, and dissolve faster into the ocean. However, the understanding of sub-millimetric bubble productions remains challenging: these bubbles are produced from the break up of much larger ones, throughout highly non-linear processes^{3,4,5}. We use direct numerical simulations in both homogeneous isotropic turbulence and in an extensional flow to built a population model, going from the fate of individual filaments to the multi-scale break-up statistics of large bubbles in turbulence. Combining numerical and experimental, I will show how that sub-Hinze bubble size distribution originates from the break-up of gas filaments, on a timescale controlled by capillarity instability.

*ESPCI, CNRS, PSL University, Sorbonne-U., UPC., Paris, France, EU

†Mechanical & Aerospace Engineering, Princeton U., US

‡ETH Zurich, Switzerland

§Oxford University, UK

¶LadHyX, Ecole Polytechnique, CNRS, Palaiseau, France, EU

||High Meadows Environmental Institute, Princeton U., US

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