

# A Dynamical Transport Theory of Wall-Bounded Turbulent Flows

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There are few theories that fully describe the turbulence in wall-bounded flows. Most rely on modelling (eddy viscosity, Reynolds stress) or approximations (large-eddy, restricted non-linear) with varying degrees of agreement with data. In a recent series of works<sup>1-3</sup>, we demonstrate that by applying the conservation principles to a control volume moving with the mean flow turbulent flows are amenable to dynamical analysis. One outcome is the transport equation for the Reynolds shear stress:

$$\frac{d(u'v')}{dy} = -C_{11}U \frac{d(u'^2)}{dy} + C_{12}U \frac{dv'^2}{dy} + C_{13} \frac{d^2u'}{dy^2} \quad (1)$$

Other components of the Reynolds stress tensor can be written in a similar manner, which in conjunction with Reynolds-averaged Navier-Stokes equation can be used to complete prescription of wall-bounded turbulent flows. In addition, self-similar behaviour appears in the gradient structures, which will be discussed in the full paper.

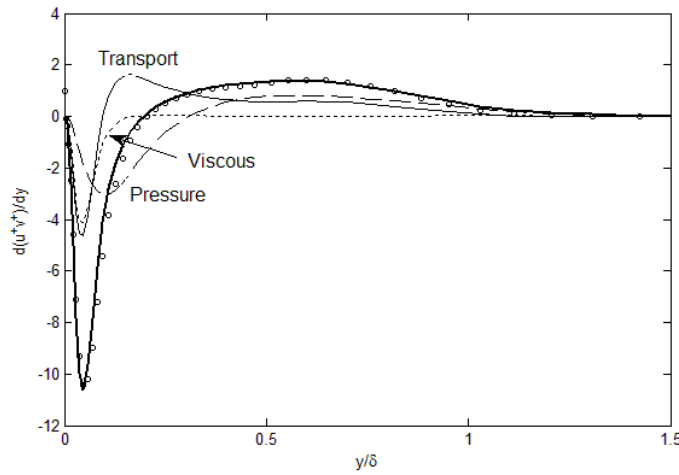


Figure 1. Validation of the turbulent transport equation (Eq. 1) with DNS data. Transport ( $C_{11}$  term), pressure ( $C_{12}$ ) and viscous ( $C_{13}$ ). These three processes combine to form  $du'v'/dy$  structure.

<sup>1</sup>Lee, *Physics of Fluids*, **33**, 055105 (2021).

<sup>2</sup>Lee, *Progress in Turbulence IX*, 237 (2022).

<sup>3</sup>Lee and Park, *Entropy*, **21**, 11 (2021).

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