Emergent elastic inertial range from smooth velocity fields in low *Re* polymeric flows

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The addition of polymers to a Newtonian fluid is well known to modify the flow characteristics. The question of precisely how polymers modify the flow of a solvent fluid is still a puzzling one, both at high and low Re numbers. We address this question for low Re flows using the commonly adopted Oldroyd-B model of polymers. We show that dilute polymer solutions, at low Re numbers, exhibit an extended emergent universal scaling regime: the *elastic range*. This behaviour of low *Re* polymeric flows holds certain similarities to classical high Re, Newtonian turbulence whilst also breaking the analogies at other times. At low Re, even though the scale-by-scale non-linear energy transfer is absent, we still find the evidence of intermittency which manifests in the deviation of structure function scaling exponents from the diffusive prediction $\zeta_p = p$. The distributions of velocity increments, consequently, show strong non-Gaussian fluctuations. However, despite intermittency, the fluid velocity fields still remain smooth and show a universal k^{-4} scaling for the energy spectrum E(k)in the elastic range. We conclude that polymeric flows, at low Re numbers, exhibit emergent universal, intermittent *elastic turbulent* states. However, purely elastic turbulence is distinct from classical, Newtonian turbulence in the fact that instabilities are driven by fluid-polymer interactions rather than the non-linear energy flux.



Figure 1: Two-dimensional snapshots of the three-dimensional fields of the normalised (a) fluid dissipation field $\epsilon_f/\langle \epsilon_f \rangle$ and (b) the corresponding polymer dissipation field, $\epsilon_p/\langle \epsilon_p \rangle$.

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